Most recent update: October 24, 2023

## RightStart™ Mathematics

# Corrections and Updates for Grade 6 Lessons and Worksheets, second edition

| LESSON/    | WORKSHEET/S    | SOLUTIONS      | CHANGE<br>DATE | CORRECTION OR UPDATE  |
|------------|----------------|----------------|----------------|---|
| Objectives |                |                | 10/24/2023     | Objectives were added to the Lesson book. See attached PDF.   |
| Lesson 9   |                |                | 10/09/2018     | Hexagram is a special six-point star based on a hexagon.  |
|            | Worksheet 10-3 | Solutions 10-3 | 10/09/2018     | Hexagram's definition is a closed six-point figure.   |
|            | Worksheet 15   |                | 10/10/2018     | Measurements for the rectangles are off. See attached PDF.  |
|            | Worksheet 27-1 |                | 11/20/2018     | Lengths for the lines to measure for Questions 6-10 are off slightly. See attached PDF.   |
|            | Worksheet 28   |                | 11/20/2018     | Measurements of the rectangle and centimeter lines are off slightly. See attached PDF.  |
|            |                | Solutions 32   | 12/17/2019     | The second equation for Problem 1B should be $4 \times 4 - 1 = 15$ , not $4 \times 4 = 16$ . The second equation for Problem 1C should be $5 \times 5 - 1 = 24$ , not $5 \times 5 = 25$ .   |
|            | Worksheet 33-2 | Solutions 33-2 | 01/03/2019     | Question 14 answer is Worksheet 32, not Worksheet 31. Question 15 has been added. See attached PDF.   |
| Lesson 35  |                |                | 01/03/2019     | The wording for the paragraph under Worksheet 35-1 has changed. It now reads, "This worksheet will have you measuring in hundredths. Your ruler only has markings for tenths, so you will be estimating the hundredths measurement. Use your best judgement to make your estimate. Complete the worksheet now." |
|            | Worksheet 35-1 |                | 11/20/2018     | Question 4 gives the wrong width measurement. It should be 2.493, not 2.927. See attached PDF.  |
|            |                | Solutions 35-1 | 01/03/2019     | The second calculation in Problem 1 should be $A = 2 \times 1 = 2$ in <sup>2</sup> , not $A = 3 \times 1 = 3$ in <sup>2</sup> .   |
| Lesson 37  |                |                | 01/03/2019     | The list of materials needs to include the Casio Calculator fx-300MS.   |
| Lesson 38  |                |                | 11/19/2018     | In the first paragraph and the second to last paragrah, the worksheet referenced should be Worksheet 36, not 34 and 35.   |
|            | Worksheet 39-1 | Solutions 39-1 | 03/27/2019     | Changed some of the matching terms and Questions 10 and 11. See attached PDFs.  |
|            |                | Solutions 39-3 | 01/03/2019     | Question 25 measurements should be 38 mm, not 39, and 48 mm, not 49. Area calculates to 1824 mm <sup>2</sup> , not 1911 mm <sup>2</sup> .   |
|            |                | Solutions 39-4 | 01/03/2019     | Question 31-33 measurement should be 74 mm, not 73. Area calculates to 4921 mm <sup>2</sup> , not 4854.5 mm <sup>2</sup> .  |
|            | Worksheet 40-1 | Solutions 40-1 | 08/01/2021     | In Question 14, the figure is missing the marks indicating the two halves of the base of the triangle are the same. See attached pdf.   |
|            | Worksheet 40-1 | Solutions 40-1 | 11/07/2022     | Question 14, choice "a" has been changed to perpendicular, not line of symmetry. Answer is still circled. See attached pdf.   |

|           |                | Solutions 40-3 | 11/10/2022 | Question 31 should have 4 of the 6 triangles of the hexagon shaded as shown here, not 5 triangles shaded.  |
|-----------|----------------|----------------|------------|--|
|           |                | Solutions 41-3 | 01/03/2019 | Question 32 measurements should be 52 mm, not 53, 33 mm, not 32, and 29 mm, not 28. Perimeter calculates to 230 mm, not 229 mm.  Question 34 measurements should be 2.0 in., not 2.1. Perimeter calculates to 7.3 cm, not 7.4 cm.  |
| Lesson 44 |                |                | 11/25/2019 | In the second heading, third paragraph should read "Using symbols, the area of the hexagon is twice the area" not octagon.   |
|           |                | Solutions 44-2 | 11/25/2019 | The last solution, #6, should read "A (rectangle)", not A (square).  |
|           | Worksheet 50-2 | Solutions 50-2 | 01/03/2019 | An additional question has been added. See attached PDFs.  |
|           | Worksheet 50-2 |                | 05/20/2020 | The solutions, rather than the worksheet itself, was included in the worksheets book and document See attached PDF.  |
|           | Worksheet 53-1 |                | 01/03/2019 | Changed the second definition listed to "quadrilateral with one and only one set of parallel lines", not "parallelogram with one and only one set of parallel lines. See attached PDF.   |
|           |                | Solutions 53-1 | 01/03/2019 | Problem 10 measurement should be 2.4 in., not 2.5. Perimeter calculates to 6.1 in, not 6.2 in and 15.5 cm, not 15.7 cm.  |
|           |                | Solutions 53-2 | 01/03/2019 | Problem 20 measurement should be 6.8 cm, not 6.9. Area calculates to 39.1 cm <sup>2</sup> , not 39.6 cm <sup>2</sup> .   |
| Lesson 55 |                |                | 01/03/2019 | The game for the day should use a target number of 180.  |
|           |                | Solutions 62   | 01/22/2019 | Question 5 answer should read 3 mm, not 3 cm.  |
|           | Worksheet 71-1 | Solutions 71-1 | 04/17/2020 | In Problem 2, the size of the television has been updated from 18" by 14.4" to 48" by 41.8" to make the measurements more realistic. Calculated height changed from 10.8" to 23.6". Problem 3 final answer should be 13.92, not 13.97, which both round to 14.0.   |
|           | Worksheet 74-1 | Solutions 74-1 | 04/17/2020 | The definitions for Questions 1-8 had multiple errors. Wording as well as order have changed. See PDFs for the Worksheet as well as the Solutions.   |
|           | Worksheet 75-1 | Solutions 75-1 | 04/17/2020 | The definition for trapezoid should be a quadrilateral with one and only one set of parallel lines, not parallelogram.   |
|           |                | Solutions 76-2 | 02/28/2019 | Question 21 answer should read 122°, not 58°.  |
|           | Worksheet 76-3 | Solutions 76-3 | 04/04/2020 | Problem 24 answer "a" should be 9.1, not 10.6 and answer "b" should be 10.6, not 9.1. The two answers were transposed. Question 31 should read "If the area of $\Delta TLG = 630 \text{ km}^2$ , what is the area of $\Delta NGI$ ? Answer is 1890 km². Question 32 should read "If line segments $GN + NA = 25 \text{ mm}$ , what is line segments $TN + NI$ ?" Answer is 50 mm. There were a few incorrect and/or illogical variations of this question and answer in some of the printings. |
| Lesson 80 |                |                | 02/08/2022 | The 4-in-1 ruler should be listed as a needed material.  |
|           | Worksheet 87-1 | Solutions 87-1 | 03/27/2019 | Order of the matching terms has been changed. The circles used for Questions 11 and 12 were off and have been corrected. See attached PDF.   |
|           | Worksheet 90-2 | Solutions 90-2 | 06/03/2019 | Question 9 uses the information from Problem 7, not Problem 6.   |
| L         |                |                | ı          |  |

|            |                 | Solutions 98-2  | 03/25/2020 | Problem 7 is missing some of the formula (in printings from April 2019 to March 2020). Second line for the area of the small circle should read: $A(sm) = \pi \times .9^2$ . Also, $r = 1.8$ cm is missing.  |
|------------|-----------------|-----------------|------------|--|
|            |                 | Solutions 99    | 04/17/2020 | The perimeter for Problem 5 should be 41.1 m, not m <sup>2</sup> .   |
|            |                 | Solutions 102   | 04/04/2020 | For Problem 2, the area for the 12" pizzas should be 113.1 in <sup>2</sup> , not 113 in <sup>2</sup> . The area for the 16" pizza should be 201.1 in <sup>2</sup> , not 201 in <sup>2</sup> .  For Problem 7, the total cost for four 16" pizzas is \$59.96, not \$59.69.  |
|            | Worksheet 103-1 | Solutions 103-1 | 04/10/2019 | The third definition should read "formula for the perimeter of a rectange" not "formula for the perimeter of a parallellogram".  |
|            | Worksheet 103-2 | Solutions 103-2 | 06/03/2019 | The prices Problems 16 have been changed to MN 20 cm = \$12.95, MN 25 cm = \$13.55, ND 20 cm \$12.53, and ND 25 cm \$12.95. See attached PDFs.   |
|            |                 | Solutions 104-1 | 04/04/2020 | The answer for Question 8 should be 1:2, not 2:1. The answer for Question 9 should be 4:1, not 1:4. The second sentence in the second paragraph of the notes should say "The ratio of mdT to IgT, 1:2, is different than the ratio of IgT to mdT, 2:1."  |
|            | Worksheet 112   | Solutions 112   | 04/28/2023 | Problem 3c should read "Translate ΔBRG (3.5, 1.5) and rotate –90° about R'." not R". And directions for 3d should read "Translate ΔBRG (8, 3) and rotate 90° about R'." not R". The solutions for the Problem 3 had mislabels. It should look like this:   |
| Lesson 113 |                 |                 | 04/22/2020 | The figures in the middle of page were labeled wrong. The left figure is reflected vertically in place, not horizontally. The right figure is reflected horizontally in place, not vertically.   |
| Lesson 120 |                 |                 | 10/10/2018 | Under the Pool table game heading, second paragraph, the second sentence should read, "In the second and third figures, the ball is reflected at 30°, then at 60°."  |
|            |                 | Solutions 121-2 | 06/03/2019 | The answer for Question 20 Elipse for maximum number of lines of symmetry is ∞, not 2.   |
| Lesson 122 | Worksheet 122-2 | Solutions 122-2 | 05/23/2023 | Lessons: Two paragraphs regarding order of rotational symmetry of 1 have been added to the top of page 138. See attached pdf.  Worksheets and Solutions: Question 7-10, the last figure's order of rotation symmetry should be 1, not none. The coloring of the figure is correct. See attached pdf for the worksheet. |
|            | Worksheet 123-2 | Solutions 123-2 | 05/23/2023 | 08/01/21: Question 6 asking about the relationship between point symmetry and the order of rotation is now Question 5. A bonus question has been added. See attached pdf. 05/23/23: Solutions have changes in Order of Rotation Symmetry and Degrees of Rotation columns. See attached pdf.                            |
|            |                 | Solutions 125-2 | 06/04/2022 | Regarding Question 18, a note has been added: Remember from Worksheet 121-2, an ellipse is considered to have two lines of symmetry; however, in the case when an ellipse is a circle, it has infinitely many lines of symmetry.   |
|            | Worksheet 126-3 | Solutions 126-3 | 06/05/2020 | Question 42 has been changed from "If area $\Delta MES = 97 \text{ km}^2$ , what is the area of $\Delta SNI$ ?" to "what is the area of $\Delta NDA$ ?" Answer is changed from 194 km <sup>2</sup> to 291 km <sup>2</sup> .  |
|            |                 |                 |            |  |

|                 | Solutions 126-8  | 01/22/2019 | The graphic for Question 78 has an error in the top right drawing. It should be as shown here.  |
|-----------------|------------------|------------|---|
|                 | Solutions 126-9  | 03/22/2020 | Question 81 should read "What is the angle of rotation between" rather tha "What is the angle of reflection between"  |
|                 | Solutions 126-10 | 05/23/2023 | Question 92, the last figure of the set, the quadrilateral, should have Order of Rot. Sym. answer of 1 with Degrees of Rotation of 360°, not 0 and 0°.  |
|                 | Solutions 127-2  | 06/03/2019 | Question 23, identification of a rhombus, should be <i>ABJF</i> and <i>CDEJ</i> . The polygons <i>FKLE</i> and <i>KBCL</i> are not rhombuses because the four sides are not equal.  |
| Worksheet 127-3 | Solutions 127-3  | 06/05/2020 | Question 42 has been changed from "If area $\Delta DIS = 82 \text{ cm}^2$ , what is the area of $\Delta DSM$ ?" to "what is the area of $\Delta DMA$ ?" Answer is changed from 164 cm <sup>2</sup> to 492 cm <sup>2</sup> . |
|                 | Solutions 127-10 | 05/23/2023 | Question 91, the last figure of the set, the quadrilateral, should have Order of Rot. Sym. answer of 1 with Degrees of Rotation of 360°, not 0 and 0°.  |

## **RIGHTSTART MATHEMATICS OBJECTIVES FOR GRADE 6**

| lame   | Year        |             | _         |
|--|-------------|-------------|-----------|
|  |             |             |           |
| Numeration   | Trimester 1 | Trimester 2 | Trimester |
| Solves problems involving whole numbers, fractions, percents, and decimals using the four operations         |             |             |           |
| Interprets and computes problems with exponents and square roots   |             |             |           |
| Rounds and compares whole numbers, fractions, and decimals   |             |             |           |
| Identifies, evaluates and applies advanced patterns, including numerical and frieze patterns                 |             |             |           |
| Solving Equations  |             | 1           | ı         |
| Writes, reads, evaluates, and solves equations with an unknown (sometimes called a variable)                 |             |             |           |
| Applies order of operations to expressions with unknown numbers (sometimes called variables)                 |             |             |           |
| and exponents  | N/A         |             |           |
| Applies distributive property  Finds and calculates the percent of a part or finds a whole when given a part | IN/A        |             |           |
| Calculates perimeter and area of triangles, quadrilaterals, and polygons, both regular & irregular           |             |             |           |
| Problem Solving  |             |             |           |
| Solves multi-step real-world and mathematical problems involving rational numbers                            |             |             |           |
| Uses reasoning to write and solve real-world problems  |             |             |           |
| Finds multiple ways to solve problems  |             |             |           |
| Ratios   |             |             | •         |
| Understands, calculates, and applies ratios to lines, shapes, and related quantities                         |             |             |           |
| or measurements  |             |             |           |
| Finds missing values in a table by using ratio reasoning   |             |             |           |
| Solves unit rate problems involving measurement and pricing  | N/A         |             |           |
| Measurement  |             | •           |           |
| Uses appropriate techniques and tools to accurately measure and draw lines and shapes                        |             |             |           |
| Converts between metric and U.S. Customary systems   |             |             |           |
| Identifies and measures angles of existing shapes and draws shapes with specific                             | N/A         |             |           |
| angle measurements   |             |             |           |
| Understands and applies four properties of angles, i.e., complementary, supplementary,                       | N/A         |             |           |
| vertical angles, and intersecting parallel lines   |             |             |           |
| Coordinate System  Draws polygons in a coordinate system   | N/A         | N/A         | 1         |
| Translates, rotates, and reflects shapes in a coordinate system  | N/A         | N/A<br>N/A  |           |
| Uses midpoints to find new coordinates of transformed shapes   | N/A         | N/A         |           |
| Understands and plots positive and negative numbers on a line or grid  | N/A         | N/A         |           |
| Statistics and Probability   | 14/21       | 14/11       |           |
| Collects and plots data on a number line or coordinate system  |             |             |           |
| Evaluates and summarizes data plotted on a number line or coordinate system                                  |             |             |           |
| Geometry   |             |             |           |
| Understands and uses formulas to calculate perimeter and area  |             |             |           |
| Learns, applies, and develops informal proofs of the Pythagorean theorem                                     | N/A         |             |           |
| Identifies and applies translations, reflections, and rotations  | N/A         | N/A         |           |
| Identifies, understands, constructs lines of symmetry and produces shapes with line symmetry                 |             |             |           |
| and rotational symmetry  |             |             |           |
| Identifies and classifies shapes by number of sides, side lengths, and angle measurements                    |             |             |           |
| Demonstrates understanding of four triangle congruence theorems (SSS, SAS, ASA, AAA) by                      | N/A         |             |           |
| drawing samples of each type   | NT/A        |             |           |
| Understands and applies pi, $\pi$  | N/A         |             |           |
| Identifies and calculates the center, radius, diameter, circumference, chords, and area of a circle          | N/A         |             |           |
| Experiences the joy and beauty of geometry in daily life   |             | <u> </u>    |           |
| Study Skills Understands and can explain geometric and other mathematical terms                              |             |             |           |
| Explores historic and cultural influences in math  |             |             |           |
|  |             |             |           |
| Develops independent learning skills   |             | I           |           |

Understands the importance of using available resources for independent learning

RightStart<sup>TM</sup> Mathematics Second Edition, 6

Name:

Date:

2. Use a perimeter formula and your calculator to calculate the perimeters in cm. Show your work. Use each of the three formulas at least once.

rectangles should have reminded you of finding 3. Finding all the possible measurements of the factors. List all the factors of 24.

4. What pattern do you see in the perimeters as the rectangles become closer to a square?

5. What is a formula for the perimeter of a square (h = w)? Date:

1–4. Match the following terms with the correct definitions.

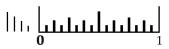
Hatching the number of parts in a fraction

Numerator shading used by engineers and designers to represent area

Denominator the number in a fraction naming the size of the part

Unit fraction fractions with a numerator of 1

5. Create a ruler below dividing it into sixteenths. Using your drawing tools, bisect the horizontal line below. At that point draw a vertical line the height of line m. Then bisect the two halves; draw lines the height of line a. Continue by bisecting the four fourths; draw lines the height of line a. Finally, bisect the eight eighths and draw those lines the height of line a.





Write the fraction for each line. Use your drawing tools to determine the length.

6.\_\_\_\_

7. \_\_\_\_\_

8.

9.

10. \_\_\_\_\_

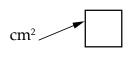
11–12. Using your drawing tools, draw a horizontal line the length indicated by the fraction. Use the ruler above as your guide.

$$\frac{5}{16}$$
 ×

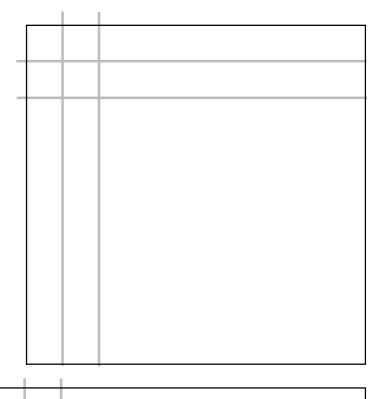
Date: \_\_\_\_\_

1. Before starting, guess which rectangle has the greater area. \_\_\_\_\_

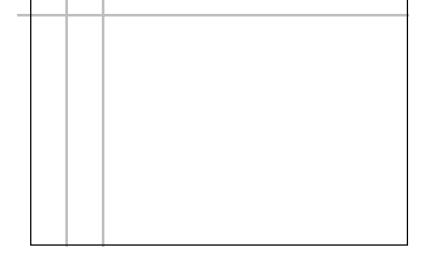
2. Fill the two rectangles below by drawing square centimeters.



A.

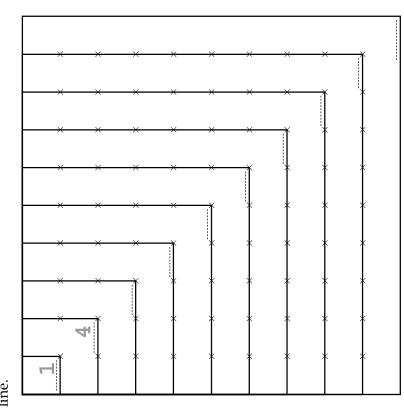


В.



3. Which of the two rectangles, A or B, has the greater area? Explain you reasoning below.

8. Below is a shortened version of the multiplication table. Find the area of each square and write the number on the dotted



9. What is special about the numbers?

10. Does the results from the previous worksheet apply?

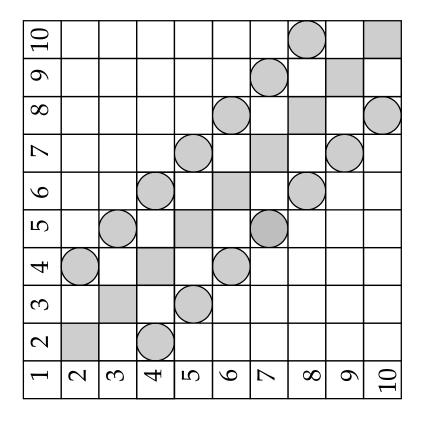
11. Find the difference between each two consecutive numbers that you wrote in the multiplication table above.

ഥ

12. Below is another version of the multiplication table. Fill in the shaded squares and circles.

Name:

Date:



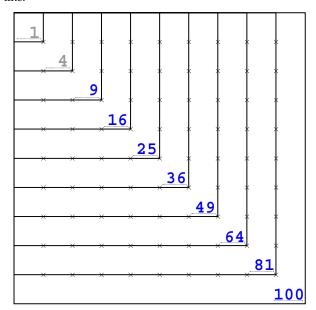
13. See the two numbers in circles next to a square. How are they related to the number in the square?

14. On what worksheet did you work with that relationship?

15. What is the formula?

Area of Consecutive Squares

8. Below is a shortened version of the multiplication table. Find the area of each square and write the number on the dotted line



9. What is special about the numbers? **They are** 

#### squares.

- 10. Does the results from the previous worksheet apply? **YES**
- 11. Find the difference between each two consecutive numbers that you wrote in the multiplication table above.

12. Below is another version of the multiplication table. Fill in the shaded squares and circles.

| 1  | 2 | 3  | 4  | 5  | 6  | 7         | 8  | 9         | 10  |
|----|---|----|----|----|----|-----------|----|-----------|-----|
| 2  | 4 |    | 8  |    |    |           |    |           |     |
| 3  |   | 9  |    | 15 |    |           |    |           |     |
| 4  | 8 |    | 16 |    | 24 |           |    |           |     |
| 5  |   | 15 |    | 25 |    | 35        |    |           |     |
| 6  |   |    | 24 |    | 36 |           | 48 |           |     |
| 7  |   |    |    | 35 |    | 49        |    | <b>63</b> |     |
| 8  |   |    |    |    | 48 |           | 64 |           | 80  |
| 9  |   |    |    |    |    | <b>63</b> |    | 81        |     |
| 10 |   |    |    |    |    |           | 80 |           | 100 |

13. See the two numbers in circles next to a square. How are they related to the number in the square?

#### Equal & one less than the square.

14. On what worksheet did you work with that relationship?

32

15. What is the formula?  $(n+1) \times (n-1) = n^2-1$ 

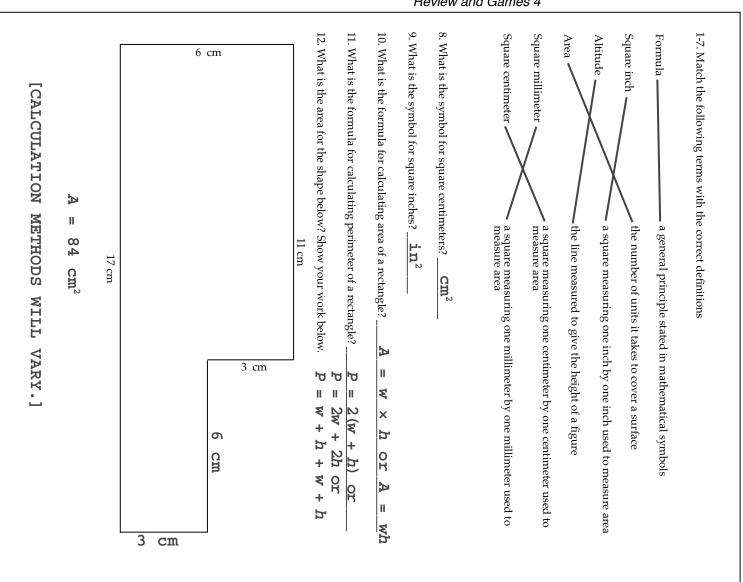
**NOTES:** Math is all about patterns. Being aware and able to find patterns will greatly help the student in their math education.

**DICTIONARY TERMS:** consecutive

| Name:   | Worksheet 35-1,<br>—— Rounding  |
|---|---|
| Date:   |   |
| Use these two quadrilaterals for the next four prob with the measurements.  | lems. Pay attention to the precision requested  |
|   |   |
| 1. Calculate the area of both quadrilaterals. <b>Measu</b>  | re to the nearest whole number using inches.  |
| 2. Calculate the area of both quadrilaterals. <b>Measu</b> to the tenths.   | <b>re to the tenths</b> using inches. Round the answers   |
| 3. Calculate the area of both quadrilaterals. <b>Measu</b> answers to the hundredths.                             | re to the hundredths using inches. Round the  |
| 4. Calculate the area of both quadrilaterals. The rectall. The parallelogram measures 2.493 inches withousandths. | etangle measures 3.139 inches wide and 1.817 inches<br>de and 1.383 inches tall. Round the answers to the |
|   |   |

CONTINUE READING THE LESSON.

| Name:                                | Worksheet 39-1,<br>————————————————————————————————————                  |
|--------------------------------------|--|
| Date:                                |  |
| 1–7. Match the following terms wit   | h the correct definitions.   |
| Formula                              | a general principle stated in mathematical symbols                       |
| Square inch                          | the number of units it takes to cover a surface                          |
| Altitude                             | a square measuring one inch by one inch used to measure area             |
| Area                                 | the line measured to give the height of a figure                         |
| Square millimeter                    | a square measuring one centimeter by one centimeter used to measure area |
| Square centimeter                    | a square measuring one millimeter by one millimeter used to measure area |
| 8. What is the symbol for square ce  | entimeters?  |
| 9. What is the symbol for square in  | ches?  |
| 10. What is the formula for calculat | ting area of a rectangle?  |
| 11. What is the formula for calculat | ing perimeter of a rectangle?  |
| 12. What is the area for the shape b | elow? Show your work below.  |
|                                      | 11 cm  |
|                                      | fi<br>fi   |
|                                      | ε<br>ο   |
| 6 cm                                 |  |
|                                      |  |
|                                      |  |
|                                      | 17 cm  |



ways. If the shape is divided vertically into two rectangles, one 11 cm by 6 cm and the other 6 cm by 3 cm, the calculation will look like this: **NOTES:** Problem 12 can be solved a number of different

$$A = wh$$
 (left rectangle) +  $wh$  (right rectangle)  
 $A = 11 \times 6 + 6 \times 3$ 

$$A = 66 + 18$$

 $A = 84 \text{ cm}^2$ 

look like this: 11 cm by 3 ft cm the other 17 cm by 3 cm, the calculation will If the shape is divided horizontally into two rectangles, one

$$A = wh$$
 (upper rectangle) +  $wh$  (lower rectangle)  
 $A = 11 \times 3 + 17 \times 3$ 

$$A = 33 + 51$$
  
 $A = 84 \text{ cm}^2$ 

the added rectangle, the calculation will look like this: Or, if the shape is made into a whole rectangle, then subtract

A = wh (whole rectangle) – wh (added rectangle)

$$A = 17 \times 6 - 6 \times 3$$

$$A = 102 - 18$$

 $A = 84 \text{ cm}^2$ 

Date: \_\_\_\_

1–11. Match the following terms with the correct definitions

Vertex the distance around a figure

Midpoint a point where the lines meet in a polygon

Perimeter the number of units it takes to cover a surface

Area middle

Numerator a closed figure with straight line segments

Parallelogram the number of parts in a fraction

Polygon a quadrilateral with two sets of parallel lines

Altitude the height of a figure

Square inch
the number in a fraction that names the sizes of the parts

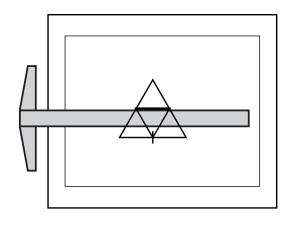
Denominator

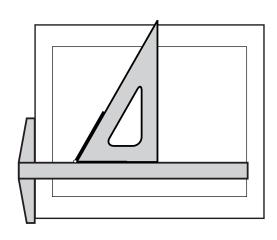
a square measuring one inch by one inch used to calculate area

Formula

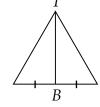
a shortcut for stating a mathematical relationship using math symbols

#### 12–13. What is wrong with these pictures?

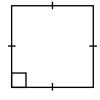




- 14. Circle all that describe the line *TB*.
  - a. Perpendicular
  - b. Horizontal
  - c. Altitude of triangle
  - d. Bisects the triangle



- 15. Circle all that describe the figure.
  - a. Parallelogram
  - b. Rectangle
  - c. Quadrilateral
  - d. Trapezoid

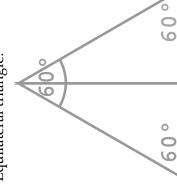


Use the two paper 30-60 triangles and arrange them to make the following figures. Then draw them with your drawing tools below. Make the shortest side of the 30-60 triangles 2.5 cm or 1 inch. For each figure, measure and write the angle of the vertices.

1. Equilateral triangle.

2. Isosceles triangle that is not equilateral.

3. Rectangle.



4-5. Two parallelograms that are neither rectangles nor mirror images of each other.

6. Quadrilateral that is not a parallelogram.

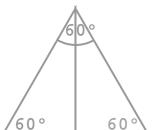
7. Which figure has the greatest area?

8. Which figures have the least perimeter?

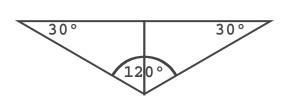
9. Which figures have the greatest perimeter?

Use the two paper 30-60 triangles and arrange them to make the following figures. Then draw them with your drawing tools below. Make the shortest side of the 30-60 triangles 2.5 cm or 1 inch. For each figure, measure and write the angle of the vertices.

1. Equilateral triangle.



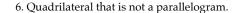
2. Isosceles triangle that is not equilateral.

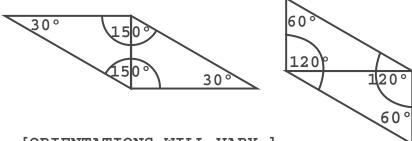


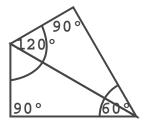
3. Rectangle.



4–5. Two parallelograms that are neither rectangles nor mirror images of each other.







[ORIENTATIONS WILL VARY.]

- 7. Which figure has the greatest area? **all the same**
- 8. Which figures have the least perimeter? rectangle, quadrilateral
- 9. Which figures have the greatest perimeter? <u>isosceles triangle</u>, <u>parallelogram</u> with shortest sides of the triangle touching

**NOTES:** Some students may struggle creating the figures with their paper triangles. Help them realize that they can flip their triangles over as well as rotate the triangles. Once the figure is discovered with the paper triangles, drawing it is made easier.

Check that the shortest side of each 30-60 triangle drawn is 2.5 cm or 1 inch. One student, Draeke, chose to write "2.5 cm" on his paper triangles to help with the construction of the figures on the worksheet.

**DICTIONARY TERMS:** goniometer

Name:

Date:

1–8. Match the following words with the correct definitions.

Straightedge shape with four sides

Octagon quadrilateral with one and only one set of parallel lines

Trapezoid eight sided polygon

Quadrilateral tool for drawing a straight line

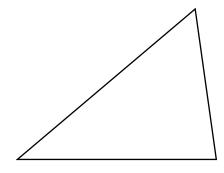
Hexagon polygon with six sides

Distributive Property quadrilateral with two sets of parallel lines

Parallelogram two equal sides

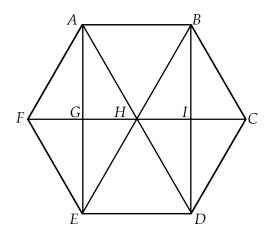
Isosceles when multiplying or dividing some numbers all by the same number, you can add the numbers first and multiply the total

- 9. How many centimeters are in 1 inch? \_\_\_\_\_
- 10. Find the perimeter of the triangle below to the nearest tenth of an inch.



11. Calculate the perimeter of the same triangle in centimeters using the calculator. P =

Use letters to identify the following shapes.



- 12. Two rhombuses:
- 13. Three rectangles:
- 14. Four trapezoids: \_\_\_\_\_
- 15. Six equilateral triangles: \_\_\_\_\_
- 16. Four isosceles triangles:
- 17. Twelve right triangles: \_\_\_\_\_\_

Date:

1–8. Match the following terms with the correct definitions

Oblique the side opposite the right angle of a triangle

Legs a line that is not parallel or perpendicular

Perfect square the two sides of a triangle opposite the hypotenuse

Hypotenuse when the square root of a number is a whole number

Pythagorean theorem a set of logical reasons for learning if a statement is true

Proof a number multiplied by itself gives the quantity

Square root the special relationship between the squares of the sides of a

right triangle

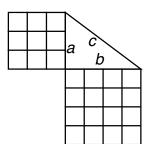
9. In the triangle on the right, how many squares

are on side *a*? \_\_\_\_\_

How many on side *b*? \_\_\_\_\_

How many on both sides? \_\_\_\_\_

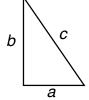
How many squares will there be on the hypotenuse? \_\_\_\_\_



10. Draw the squares onto the sides of the triangle on the right using your drawing tools. Measure to the tenths of a cm, then give the answers to the hundredths.

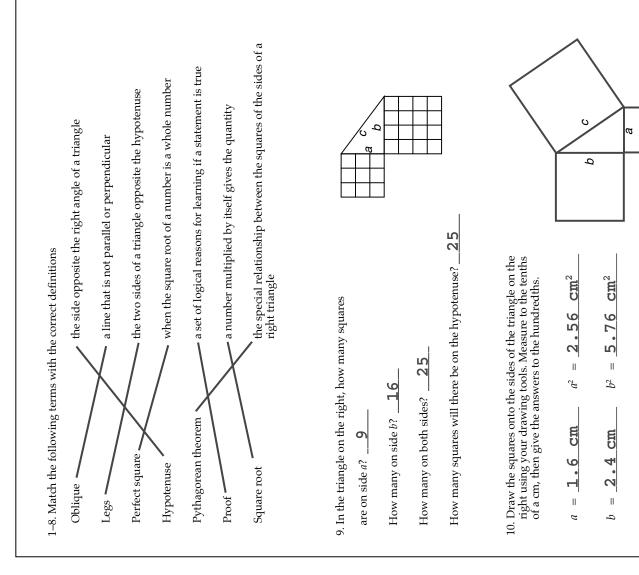
$$a =$$
\_\_\_\_\_  $a^2 =$ \_\_\_\_\_

$$c = 2.884 \text{ cm}$$
  $c^2 =$ 



11. Does  $c^2 = a^2 + b^2$ ?

**NOTES:** Make sure the student is understanding the difference between the measurements a, b, and c and the square of the numbers,  $a^2$ ,  $b^2$ , and  $c^2$ .



11. Does  $c^2 = a^2 + b^2$ ?

8.32

Ш

 $c_5$ 

00 00 40

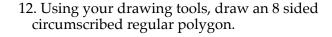
 $\parallel$ 

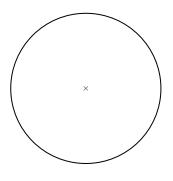
Circumscribed polygon a path made by points that extends forever

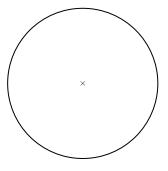
Radius an exact place, with no width, depth or height

Point a line segment with one end at the center and the other on the circle

11. Using your drawing tools, draw an 8 sided inscribed regular polygon.





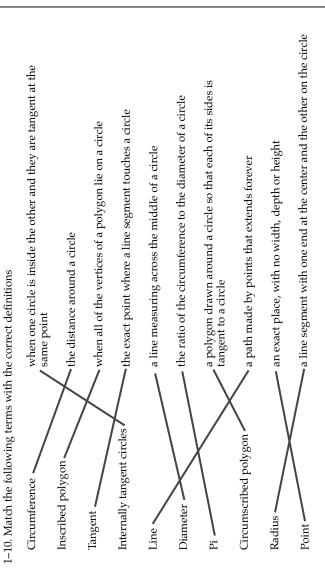


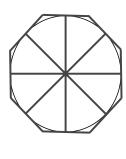
13–14. For each polygon, measure the length of a side in millimeters. Find the perimeter. Calculate the ratio of P, the perimeter of the polygon, to *D*, the diameter of the circle. Complete the chart below.

| Number of<br>Sides | Length, Side of<br>Polygon in mm | P (perimeter) of Polygon in mm | D (diameter) of<br>Circle in mm | Ratio of P to D (hundredths) |
|--------------------|----------------------------------|--------------------------------|---------------------------------|------------------------------|
| 8 Inscribed        |                                  |                                |                                 |                              |
| 8 Circumscribed    |                                  |                                |                                 |                              |

128 ÷ 40. If the student's measurements vary, check that their student that the ratio of P, perimeter, to D, diameter, is found NOTES: On Problems 13 and 14, if needed remind the by dividing the perimeter by the diameter, 120 ÷ 40 and ratio is accurate.

If the student uses tickmarks, rather than line segments as shown in Problems 11 and 12, that is acceptable.





12. Using your drawing tools, draw an 8 sided

11. Using your drawing tools, draw an 8 sided

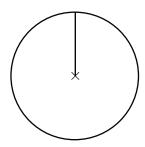
inscribed regular polygon.

circumscribed regular polygon.

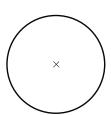
13–14. For each polygon, measure the length of a side in millimeters. Find the perimeter. Calculate the ratio of P, the perimeter of the polygon, to P, the diameter of the circle. Complete the chart below.

| Number of<br>Sides | Length, Side of<br>Polygon in mm | Length, Side of $P$ (perimeter) of $D$ (diameter) of $P$ to $D$ Polygon in mm $P$ Polygon in mm $P$ (hundredths) | D (diameter) of Circle in mm | Ratio of P to D<br>(hundredths) |
|--------------------|----------------------------------|--|------------------------------|---------------------------------|
| 8 Inscribed        | 15 mm                            | 120 mm   | 4.0 mm                       | 3.00                            |
| 8 Circumscribed    | 16 mm                            | 128 mm   | 40 mm                        | 3.20                            |

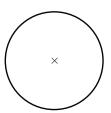
12. Draw a special square using the radius of this circle as one side. Find the perimeter and area of the square and then find the circumference and area of the circle.



- 13. Find the radius of a circle that has twice the circumference of the circle below. Draw the circle.
- 14. Find the radius of a circle that has twice the area of the circle below. Draw the circle.



×



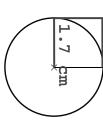
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- 15. The Vikings had a favorite snack called lefsa. It is a soft tortilla made with potatoes, flour, butter, and cream. Find the area to the nearest tenth of a square cm for each size of lefsa in Minnesota and North Dakota. Fill in the chart.
- 16. Find the price per square centimeter in tenths of a cent for each piece of lefsa.

|                       | Lefsa in Minnesota |         |  |  |  |  |
|-----------------------|--------------------|---------|--|--|--|--|
| Size                  | 20 cm              | 25 cm   |  |  |  |  |
| Price                 | \$12.95            | \$13.55 |  |  |  |  |
| Area                  |                    |         |  |  |  |  |
| Price/cm <sup>2</sup> |                    |         |  |  |  |  |

| Lefsa in North Dakota |         |         |  |  |  |
|-----------------------|---------|---------|--|--|--|
| Size                  | 20 cm   | 25 cm   |  |  |  |
| Price                 | \$12.53 | \$12.95 |  |  |  |
| Area                  |         |         |  |  |  |
| Price/cm <sup>2</sup> |         |         |  |  |  |

12. Draw a special square using the radius of this circle as one side. Find the perimeter and area of the square and then find the circumference and area of the circle.



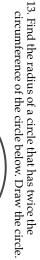
$$C = 2\pi \times 1.7$$

$$C \approx 10.7 \text{ cm}$$

$$P = 1.7 \times 4$$
  
 $P = 6.8 \text{ cm}$   
 $C = 2\pi x$   
 $C = 2\pi \times 1.7$   
 $C \approx 10.7 \text{ cm}$ 

$$A(sq) = r^{2}$$
  
 $A(sq) = 1$   
 $A(sq) = 2$ 

$$A(sq) = 1.7^{2}$$
  
 $A(sq) = 2.9$ 



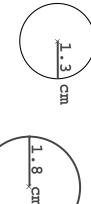
$$A(\text{sq}) = 2.9 \text{ cm}^2$$

$$A(\text{cir}) = \pi x^2$$

$$A(\text{cir}) = \pi \times 1.$$



14. Find the radius of a circle that has twice the area of the circle below. Draw the circle. A(cir) N 9 Cm<sup>2</sup> 1.72



. ნ



C(1g)C(1g)  $C(\mathrm{sm})$  $C(\mathrm{sm})$ C(sm)

16.4

Cm

8.2 × 2

П

& . 2

 $2\pi \times 1.3$ CIE

II

 $2\pi r$ 

r(1g)

2πr 16.4 2π

N

2.6

CIB

16.4

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|     | 16. Find the price per square centimeter in tenths of a cent for each piece of lefsa. |
|     | Сe  |
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|     | fsa   |
| - [ | 'n  |

15. The Vikings had a favorite snack called lefsa. It is a soft tortilla made with potatoes, flour, butter, and cream. Find the area to the nearest tenth of a square cm for each size of lefsa in Minnesota and North Dakota. Fill in the chart.

|                       | Lefsa in Minnesota | sota    |
|-----------------------|--------------------|---------|
| Size                  | 20 cm              | 25 cm   |
| Price                 | \$12.95            | \$13.55 |
| Area                  | 314.2              | 490.9   |
| Price/cm <sup>2</sup> | 4.1¢               | 2.8¢    |

| L                     | Lefsa in North Dakota | akota   |
|-----------------------|-----------------------|---------|
| Size                  | 20 cm                 | 25 cm   |
| Price                 | \$12.53               | \$12.95 |
| Area                  | 314.2                 | 490.9   |
| Price/cm <sup>2</sup> | 4.0¢                  | 2.6¢    |

practical nor likely. diameter of the snack, using a radius measurement is not is the diameter. Although it does not specifically say it is the NOTES: On Question 16, the sizes given, 20 cm and 25 cm,

### **LESSON 122: ROTATIONAL SYMMETRY**

#### **OBJECTIVES:**

- 1. To learn the terms *rotational symmetry*, *order of rotation symmetry*, and *point symmetry*
- 2. To apply rotational symmetry and point symmetry

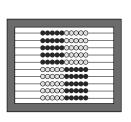
#### **MATERIALS:**

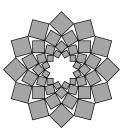
- 1. Math Dictionary
- 2. Worksheet 122, Rotational Symmetry
- 3. Tangrams
- 4. Colored pencils, optional
- 5. Math Card Games book

#### **ACTIVITIES:**

**Rotational symmetry.** Just as line symmetry refers to a line of symmetry within an object, *rotational symmetry* refers to rotation of an object. If a figure can be rotated and looks the same as before the rotation, it has rotational symmetry.

In the left figure below, the abacus has rotational symmetry; you can turn it 180° and it will look exactly as the original abacus.







In the center figure above, an image of the design (a logo) can be rotated  $30^{\circ}$  and still fit exactly on the original. Actually, it can be rotated for every multiple of  $30^{\circ}$  up to  $360^{\circ}$ , such as  $30^{\circ}$ ,  $60^{\circ}$ ,  $90^{\circ}$ , and so on, for a total of 12 times because  $360 \div 30 = 12$ . When counting the number of rotations, we only go around once so do not count anything past  $360^{\circ}$ . The number of times it can be rotated is the *order of rotation symmetry*.

The car wheel above on the right can be rotated  $72^{\circ}$  (360 ÷ 5) and four more multiples of 72 and still look like the original.

The figures below show the five counterclockwise rotations. Notice the shadow. It will help you keep track as you observe the rotations. What is the order of rotation symmetry? Answer is below.











#### **EXTRAS:**



This lily demonstrates rotational symmetry.



The leaves on a milkweed plant rotate so they receive as much sunlight as possible.

The point of rotation is usually easy to find: it's the center of the figure.

Sometimes rather than saying the order of rotation symmetry is 5, you will see the term "5-fold" or "12-fold" for the order of 12.

LESSON CONTINUES ON THE NEXT PAGE.

Answer: 5

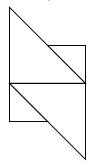
#### **ACTIVITIES:**

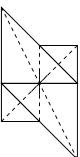
All objects have an order of rotational symmetry of 1 or more. Can you think why every object has at least an order of rotation of 1? Hint: what is  $360 \div 360$ ? It's 1!

So, in other words, you can always rotate an object completely around, 360°, and it will look the same. Therefore, everything has an order of rotation of 1 and sometimes more.

**Point symmetry.** A special case of rotational symmetry is *point symmetry*. An easy way to check for point symmetry is to rotate it 180°. If it looks the same, upside down as right side up, it has point symmetry.

To understand why it's called point symmetry, follow these steps. First construct this figure with your tangrams on top of a sheet of paper. Then rotate the paper 180° to see that the tangram design has point symmetry.





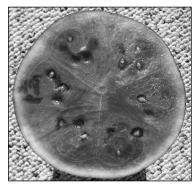
Next consider what happens if you connect the corresponding points. As you can see in the figure above on the right, the lines intersect at the center. The center also bisects each connecting line. It can be thought of as though each point is reflected through the center point. That's point symmetry.

**Worksheet 122.** The worksheet is a collection of problems applying symmetries.

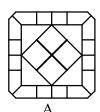
**Symmetry in logos, optional.** Collect a dozen or so logos from magazines, the internet, or products. Analyze them for symmetry.

**Today's game.** Play your choice of math card game from the *Math Card Games* book.

#### **EXTRAS:**



Watermelons also exhibit symmetry.

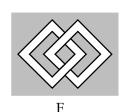


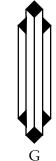












1. Which of the figures above have line symmetry? \_\_

2. Which of the figures have rotational symmetry? Give the order of rotation symmetry.

\_\_\_\_\_

3. Which of the figures have point symmetry? \_\_\_\_\_

 ${\it 4. List the seven capital letters that have rotational symmetry.}$ 

5. List the three digits that have rotational symmetry.

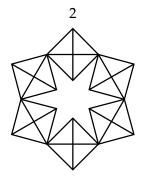
\_\_\_\_\_

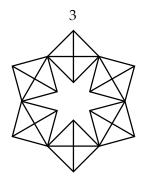
NOW NO SWIMS ON MON

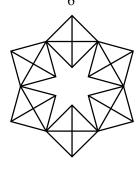
6. What did the diver read on the sign while traveling headfirst toward the water?

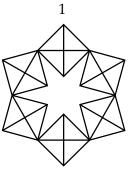
7–10. Color the squares in the figures below to show the order of rotation symmetry given.







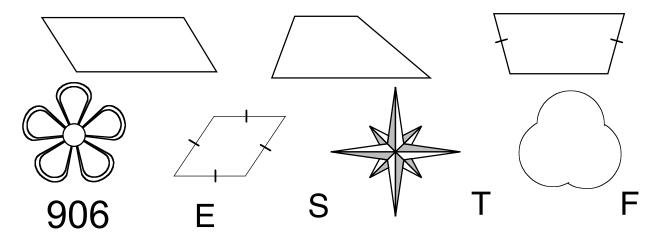




11. Color the shaded part of the logo on the right. Then color the remaining part of the logo so it has rotational symmetry. What is the order of rotation symmetry? \_\_\_\_

Date: \_\_\_\_\_

4. Consider the symmetry of each figure and fill in the table below.

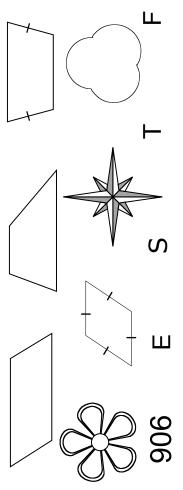


| Shape    | Line<br>Symmetry? | Point<br>Symmetry? | Rotational<br>Symmetry? | Order of<br>Rotation<br>Symmetry | Degrees of<br>Rotation |
|----------|-------------------|--------------------|-------------------------|----------------------------------|------------------------|
|          |                   |                    |                         |                                  |                        |
|          |                   |                    |                         |                                  |                        |
|          |                   |                    |                         |                                  |                        |
| <b>%</b> |                   |                    |                         |                                  |                        |
|          |                   |                    |                         |                                  |                        |
|          |                   |                    |                         |                                  |                        |
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| S        |                   |                    |                         |                                  |                        |
| Т        |                   |                    |                         |                                  |                        |
| F        |                   |                    |                         |                                  |                        |

5. What is the relationship between point symmetry and the order of rotation? \_\_\_\_\_

BONUS: Can you have rotational symmetry without line symmetry and point symmetry? \_\_\_\_\_

4. Consider the symmetry of each figure and fill in the table below.



occurs when an object has symmetry about a point only when

An object having rotational symmetry with an order of

The star is not symmetrical because of the shading.

beneficial for some students. Considering line symmetry for

**NOTES:** Approaching this table systematically may be

all figures, then point symmetry, then rotational symmetry,

etc, helps keep each definition straight.

rotated by 360 ÷ 1, which is 360 degrees. In other words, the

have no symmetry less than 2. Rotational symmetry for these

order of rotation symmetry of 1 happens with objects that

objects is trivial. Therefore, the simplest possible rotational

symmetry is of order 2.

information, when neither line symmetry nor point symmetry

For the bonus question, only looking to the chart's

exist, rotational symmetry does not appear to exist. The

second quadrilateral and the letter F both have no line

symmetry, no point symmetry, as well as no rotational

After some work, he shows that

Joshua Dill from St. Paul, MN.

symmetry.

age 14, wondered about this.

without point or line symmetry

being present.

So the answer to the bonus

rotational symmetry can exist

Question 5 can also reference the order of rotation being a

multiple of 2.

| Point<br>Symmetry? |
|--------------------|
| Yes                |
| no                 |
| no                 |
| no                 |
| yes                |
| yes                |
| no                 |
| Yes                |
| no                 |
| yes                |
| no                 |
| no                 |

consider figure B from Worksheet 122 as question is "yes." Additionally,

shown here. It has rotational symmetry without ine symmetry and point symmetry.

**DICTIONARY TERMS:** heptagon

even **1**. rotation of order exists when only

5. What is the relationship between point symmetry and the order of rotation? **Point** 

symmetry

BONUS: Can you have rotational symmetry without line symmetry and point symmetry?